

Page 1-5	Mark Scheme	Syllabus	Paper
	COSMIC CHALLENGING EXAMINATIONS – Set 1	4038	1

**7 Mark Scheme:**

- |  |    |     |
|--|----|-----|
| (i) Find gradient of AC                          | M1 |     |
| Find gradient of BC                              | M1 |     |
| Apply $m_1 m_2 = -1 \Rightarrow AC \perp BC$ .   | A1 | [3] |
| (ii) Find centre of circle                       | M1 |     |
| Find radius                                      | M1 |     |
| Equation of circle: $(x - 3)^2 + (y - 4)^2 = 25$ | A1 | [3] |

**Suggested Solution:**

(i) Gradient of AC =  $\frac{4 - (-1)}{-2 - 3} = -1$

Gradient of BC =  $\frac{4 - (-1)}{8 - 3} = 1$

Since  $m_{AC} m_{BC} = -1$ ,  $AC \perp BC$ . (ans)

(ii) AB is the diameter of the circle

Center of circle = midpoint of AB =  $\left(\frac{8 - 2}{2}, \frac{4 + 4}{2}\right) = (3, 4)$

Radius =  $\sqrt{(-2 - 3)^2 + (4 - 4)^2} = 5$

Equation of circle:  $(x - 3)^2 + (y - 4)^2 = 25$  (ans)

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**8 Mark Scheme:**

- |   |    |     |
|---|----|-----|
| (i) $2^5 + {}^5C_1 2^4 (-4x) + {}^5C_2 2^3 (-4x)^2$ |    |     |
| $32 - 320x + 1280x^2$                               | B3 | [3] |
| (ii) $32a = 96, a = 3$                              | B1 |     |
| $-320a + 32b = -1120$                               | M1 |     |
| $b = -5$  | A1 |     |
| $1280a - 320b = c$                                  | M1 |     |
| $c = 5440$  | A1 | [5] |

**Suggested Solution:**

(ii)  $(a + bx)(2 - 4x)^5 = 96 - 1120x + cx^2 + \dots$

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	<b>COSMIC CHALLENGING EXAMINATIONS – Set 1</b>	<b>4038</b>	<b>1</b>

$$(a + bx)(32 - 320x + 1280x^2 + \dots) = 96 - 1120x + cx^2 + \dots$$

$$32a - 320ax + 1280ax^2 + 32bx - 320bx^2 + 1280bx^3 + \dots = 96 - 1120x + cx^2 + \dots$$

Comparing coefficients

$$32a = 96 \Rightarrow a = 3 \text{ (ans)}$$

$$-320a + 32b = -1120 \Rightarrow b = -5 \text{ (ans)}$$

$$1280a - 320b = c \Rightarrow c = 5440 \text{ (ans)}$$

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## 9 Mark Scheme:

- (i)  $\ln y = mx^2 + c$  M1  
 $m = -2$  A1  
Substitute  $\ln y = 2, x^2 = 1$  into  $\ln y = mx^2 + c \Rightarrow c = 4$  A1  
 $y = e^{-2x^2 + 4}$  A1 [4]
- (ii) Applies  $\lg$  to both sides of the equation M1  
Applies rules of logarithms  $[\log xy = \log x + \log y]$  M1  
Applies rules of logarithms  $[\log_a x^r = r \log_a x]$  M1  
 $Y = \lg y, m = 2 \lg b, X = x, c = \lg a$  A1 [4]

### Suggested Solution:

- (i)  $\ln y = mx^2 + c \Rightarrow m = \frac{-14 - 2}{9 - 1} = -2$   
Substitute  $\ln y = 2, x^2 = 1$  into  $\ln y = mx^2 + c$ :  
 $2 = (-2)(1) + c \Rightarrow c = 4$   
 $\ln y = -2x^2 + 4 \Rightarrow y = e^{-2x^2 + 4} \text{ (ans)}$
- (ii)  $y = ab^{2x} \Rightarrow \lg y = \lg ab^{2x} \Rightarrow \lg y = \lg a + \lg b^{2x} \Rightarrow \lg y = 2x \lg b + \lg a$   
 $Y = \lg y, m = 2 \lg b, X = x, c = \lg a \text{ (ans)}$

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## 10 Mark Scheme:

- (i) Applies quotient or product rule M1  
 $\frac{dy}{dx} = \frac{26}{(x+5)^2}$  A1  
Numerator  $\neq 0$  for any value of  $x \rightarrow$  No turning points. B1√ [3]
- (ii)  $P\left(\frac{1}{5}, 0\right)$  B1